**Course Name:** Advanced Numerical Methods in Geomechanics

**Course Number:** 20409

Credit: 3

## **Course Content (outline):**

## 1. Advanced Topic In FEM

- 1.1 Lagrangian and Serendipity Elements
- 1.2 Rayleigh-Ritz Method as Theoretical Basis for FEM
- 1.3 Solution Convergence in FEM Modeling
- 1.4 Selection of The Order of Numerical Integration
- 1.5 Non-Conforming Elements and Patch Test
- 1.6 Zero-Energy Modes

## 2. Nonlinear Analysis In Solid Mechanics

- 2.1 Iterative and Incremental Approaches in Nonlinear Analysis
- 2.2 Material Nonlinearity
- 2.3 Application of Nonlinear Elastic Models
- 2.4 Application of Elasto-Plastic Models
- 2.5 Application of Time-Dependent Models
- 2.6 Geometric Nonlinearity
- 2.7 Definitions of Stress and Strain in Large Deformations
- 2.8 Total Lagrangian Formulation
- 2.9 Updated Lagrangian Formulation

#### 3. Dynamic Analysis

- 3.1 Static, Quasi-static, and Dynamic Problems
- 3.2 FEM Form of Equation of Motion
- 3.3 Direct Integration Methods
- 3.4 Mode Superposition
- 3.5 Mass and Damping Matrices
- 3.6 Mesh Configuration and Boundary Conditions
- 3.7 Application of Load in Dynamic Analysis

## 4. Numerical Simulation of Discontinuities

- 4.1 Weak and Strong Discontinuities
- 4.2 Smeared and Discrete Approaches in Modeling Cracks
- 4.3 Existing Cracks and Propagating Cracks
- 4.4 Crack Modes (Tensile, Shear, Mixed)
- 4.5 Application of Interface Elements in Discrete Crack Modeling
- 4.6 Simulation of Fluid Flow inside Cracks

# 5. Coupled Problems

- 5.1 Difference between Coupled and Uncoupled Problems
- 5.2 Examples of Coupled Problems and Their Governing Equations
- 5.3 Formulation of a Hydro-Mechanical Problem
- 5.4 Formulation of a Thermo-Hydro-Mechanical Problem
- 5.5 Two-Phase Flow in a Deforming Porous Medium

# 6. Other Numerical Methods

- 6.1 Boundary Element Method
- 6.2 Discrete Element Method
- 6.3 Extended Finite Element Method
- 6.4 Spectral Elements Method
- 6.5 Mesh-Free Methods

# **References:**

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- Bathe, K.J., "Finite Element Procedures in Engineering Analysis", (1996), Prentice Hall
- Zienkiewicz & Taylor, "The Finite Element Method", vol. 2, 4<sup>th</sup> Edition, (1989), McGraw Hill
- Smith, I.M., & Griffith, D.C., "Programming the Finite Element Method", 2<sup>nd</sup> Edition (1992), John Wiley & Sons
- Zienkiewicz, O.C., Chan, A.C.H, Pastor, M., Schrefler, B.A., Shiomi, T., "Computational Geo-mechanics, with special reference to earthquake engineering", John Wiley, (1999)
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